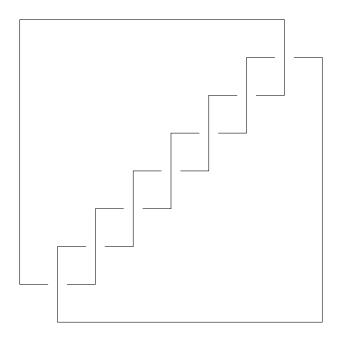
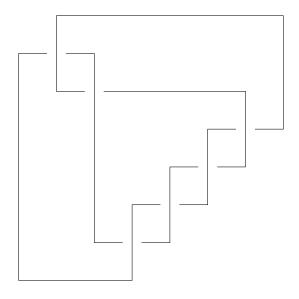
## Revision Question 3 — 02/05/14

The knot  $7_1$ , known as the septafoil, is pictured below.



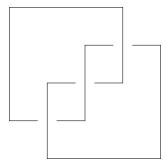
a) There is an integer p such that  $7_1$  is m-colourable if and only if  $p \mid m$ . Find p. Justify your answer. [8 marks]

The knot  $6_1$ , known as the  $stevedore\ knot$ , is pictured below.



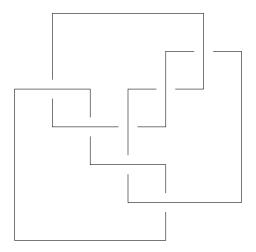
- b) Find a 15-colouring of  $6_1$ . [6 marks]
- c) Is  $6_1$  isotopic to  $7_1$ ? Justify your answer. You may quote without proof any results from the course. [3 marks]

The knot  $\mathbf{3}_{1}$ , the trefoil, is pictured below.



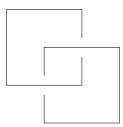
d) Prove that  $6_1$  is not isotopic to  $3_1$ . You may quote without proof any results from the course. [12 marks]

The link  $7_5^2$  is pictured below.



e) What is the linking number of  $7_5^2$ ? [5 marks]

The link  $2_1^2$ , the Hopf link, is pictured below.



- f) Prove that  $7_5^2$  is not isotopic to  $2_1^2$ . Justify your answer. You may quote without proof any results from the course. [3 marks]
- g) Can your answer to e) be used to prove that  $7_5^2$  is not isotopic to the unlink with two components? [3 marks]